dicular respectively to  $O(2^{vii})-O(2^{vi})$ . The thermal motion of the O atoms, especially of O(2), is nearly isotropic. The assumption of a preferred expansion of the thermal vibration ellipsoids of the Te atoms in the directions of the largest main axes by heat treatment may explain the stronger temperature dependence of the *c* axis as compared with the *a* axis.

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## Structures of $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>, (Mn<sub>0.983</sub>Fe<sub>0.017</sub>)<sub>2</sub>O<sub>3</sub> and (Mn<sub>0.37</sub>Fe<sub>0.63</sub>)<sub>2</sub>O<sub>3</sub> and Relation to Magnetic Ordering

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The crystal structures of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> and of (Mn<sub>1-x</sub>Fe<sub>x</sub>)<sub>2</sub>O<sub>3</sub>, x=0.017 and 0.63 have been refined by least-squares calculations from three-dimensional X-ray diffraction data obtained with a Buerger– Supper–Pace–Picker diffractometer. At 25 °C, crystals of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> belong to space group *Pcab* ( $D_{2h}^{15}$ ) with a=9.4157 (3), b=9.4233 (3), c=9.4047 (3) Å; (Mn<sub>0.983</sub>Fe<sub>0.017</sub>)<sub>2</sub>O<sub>3</sub> and (Mn<sub>0.37</sub>Fe<sub>0.63</sub>)<sub>2</sub>O<sub>3</sub> belong to *Ia3* ( $T_h^7$ ) with lattice constants 9.4146 (1) and 9.4126 (3) Å respectively. Interatomic distances and angles in (Mn<sub>0.983</sub>Fe<sub>0.017</sub>)<sub>2</sub>O<sub>3</sub> are equal to the analogous average distances and angles in  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>. There appears to be significantly less distortion of the oxygen polyhedra about the 24(*d*) sites in (Mn<sub>0.37</sub>Fe<sub>0.63</sub>)<sub>2</sub>O<sub>3</sub> than in (Mn<sub>0.983</sub>Fe<sub>0.017</sub>)<sub>2</sub>O<sub>3</sub>. Evidence is presented in support of the suggestion that the antiferromagnetic ordering temperatures depend on the allowed distortion of the Mn<sup>3+</sup> ion surroundings. The results on  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> differ in minor respects from those of Norrestam (*Acta Chem. Scand.* (1967). **21**, 2871].

### Introduction

This work was undertaken to gain further insight into the crystallographic and magnetic behavior of what appears to be a unique system,  $(Mn_{1-x}Fe_x)_2O_3$ . Early investigators (Zachariasen, 1928; Pauling & Shappell, 1930) believed  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> to be cubic and to have the same crystal structure as the mineral bixbyite ( $x \simeq 0.5$ ). This conclusion was drawn on the basis of X-ray powder diffraction photography with Fe K $\alpha$  radiation. Our own work indicates that the deviation from cubic symmetry in such photographs is barely detectable, and perhaps only if one already knows that the Mn<sub>2</sub>O<sub>3</sub> is not cubic. Further, less than one cation % Fe<sup>3+</sup> impurity would make the compound cubic at room temperature (Grant, Geller, Cape & Espinosa, 1968).

Some structural work on  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> has also been done with neutrons both at room temperature (Fert, 1962;\* Hase, 1963) and at very low temperature (Cable, Wilkinson, Wollan & Koehler, 1957). No deviation from cubic symmetry was noted by these investigators but the magnetic structure at low temperatures appeared to be very complex.

<sup>\*</sup> In a previous paper (Geller, Romo & Remeika, 1967) we pointed out that Fert's interatomic distances for  $Mn_2O_3$  could not be correct. Fert's parameter values agree well with those found for  $(Mn_{0.983}Fe_{0.017})_2O_3$ . Thus it appears that he calculated the distances for  $Mn_2O_3$  incorrectly.

At room temperature, the distortion of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> from cubic symmetry is observable in a powder photograph taken with  $Cr K\alpha$  radiation. We reported (Geller, Cape, Grant & Espinosa, 1967) that the maximum symmetry the phase could have was orthorhombic. Not long after this report, single crystals of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> were grown by Espinosa and the crystals were indeed found to be orthorhombic, space group Pcab (Geller, Grant, Cape & Espinosa, 1968). Norrestam (1967) describes a method whereby he obtained a single crystal of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> by appropriate annealing of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> powder. He had difficulty with twinning, but did finally find a crystal in which it was negligible. Although several of the crystals, of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> and  $(Mn_{1-x}Fe_x)_2O_3$ , grown by Espinosa were examined with single-crystal X-ray photography, no twinning was observed. Norrestam (1967) has reported the structure of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> and except for minor discrepancies to be discussed later, the results reported here confirm his.

The  $(Mn_{1-x}Fe_x)_2O_3$  system has been studied to various extents by several workers (Zachariasen, 1928; Pauling & Shappell, 1930; Wretblad, 1930; Montoro, 1940; Mason, 1943; Dachs, 1956; Hase & Meisel, 1966; Hase, Kleinstück & Schulze, 1967; Hase, Brückner, Tobisch, Ulrich & Wegerer, 1969;\* Grant *et al.*, 1968). Until recently, specimens were prepared by solid state reaction and structural investigations were made on powders. The mineral bixbyite has also been studied (see several of preceding references), but in this case, also, the structural investigations were made on powders. Bixbyite is cubic, as all investigators agree, and belongs to space group *Ia3*.

Initially our susceptibility and Mössbauer spectroscopic studies (Geller, Grant, Cape & Espinosa, 1967) were made on powder specimens prepared by solid state reaction. These studies produced some anomalies which were explained when homogeneous crystals were obtained (Grant *et al.*, 1968). Crystals have been grown by Espinosa, with compositions ranging from 0 to 63 cation per cent  $Fe^{3+}$ .\* These enabled us to determine the phase diagram, including magnetic phases of the system (Grant *et al.*, 1968).

#### Experimental

All the crystals used in this investigation were grown by Espinosa (1970) by a flux method. The three crystals studied had x=0.00, 0.017 and 0.63, the second and third compositions having been ascertained by chemical analysis. The crystals were ground into spheres (Bond, 1951) of radius 0.16, 0.10, and 0.11 mm respectively. Lattice constants of these specimens were determined with a Bond (1960) spectrometer. Crystal data for the specimens are given in Table 1.

The intensity data were collected with a Buerger-Supper-Pace-Picker automatic diffractometer; Mo K $\alpha$  radiation and balanced Zr and Y filters were used. In all cases, the data collected were those included within  $2\theta = 60^{\circ}$ . For the  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>, the *b* axis was the rotation axis and all the data within the hemisphere (and  $2\theta \le 60^{\circ}$ ) were collected. For the two cubic iron-containing specimens, intensities of only independent reflections were collected.

The continuous scan mode was used with  $1 \cdot 0^{\circ} \min^{-1}$  scan rate and scan interval of  $2^{\circ}$  or more. Background counts were taken at the beginning and end of the scan interval at  $\frac{1}{4}$  the scan time of each reflection.

Relative  $|F_o|^2$  were obtained by application of the Lorentz-polarization-Tunell and absorption factors (Bond, 1959) to the intensities. For  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>, the relative  $|F_o|^2$  were averaged, from which 1209 independent  $|F_o|$  were obtained. A total of 207 independent inten-

\* Earlier, crystals of  $(Mn_{0.5}Fe_{0.5})_2O_3$  had been grown by Banks & Kostiner (1966) by a very different technique.

Most probable space group	$Mn_2O_3$ $Pcab^* (D_{2h}^{15})$	$(Mn_{0.983}Fe_{0.017})_2O_3$ Ia3 (T <sub>h</sub> 7)	$(Mn_{0.37}Fe_{0.63})_2O_3$ Ia3 $(T_h^7)$
Lattice constants (Å)	a=9.4157 (3) b=9.4233 (3) c=9.4047 (3)	a=9·4146 (1)	a = 9.4126 (3)
Unit-cell volume (Å <sup>3</sup> ) Formula weight Unit-cell contains	834·45 157·87 32 Mn <sup>3+</sup> 48 O <sup>2-</sup>	834·46 157·91 31·46 Mn <sup>3+</sup> 0·54 Fe <sup>3+</sup> 48 O <sup>2-</sup>	833·93 159·02 11·84 Mn <sup>3+</sup> 20·16 Fe <sup>3+</sup> 48 O <sup>2-</sup>
Calculated density (g.cm <sup>-3</sup> ) $\mu$ , Mo K $\alpha$ (cm <sup>-1</sup> )	5·025 119·45	5·026 119·76	5.065 131.64
Systematic absences	hol with $h \neq 2n$ hk0 with $k \neq 2n$ Okl with $l \neq 2n$	hkl with $h+k+l \neq 2n$ $0kl$ with $k, l \neq 2n$ $(hk0 \text{ with } h, k \neq 2n$ $h0l$ with $h, l \neq 2n$ )	

Table 1. Crystal data

\* This space group designation adheres to the convention c < a < b. See also last section of Discussion.

<sup>\*</sup> We find no experimental support of the contention by these authors that for  $0.01 < x \le 0.38$  in  $(Mn_{1-x}Fe_x)_2O_3$ , the space group is  $I2_13$  instead of Ia3.

∝-Mn₂O₃*						10	)5 ×		
	X	ų	Z	$\beta_{11}$	$\beta_{22}$	$\beta_{33}$	B12	$\beta_{13}$	$\beta_{23}$
Mn(1)	0	0	0	96 (12)	98 (12)	90 (12)	4 (3)	22 (2)	4 (1)
5	0	0	Ŧ	127 (12)	127 (12)	100 (12)	12 (7)	12 (7)	6 (7)
<u>(</u> 3)	0.28479 (10)	0-25253 (5)	<u> </u>	134 (11)	156 (10)	206 (10)	-5 (3)	19 (3)	- 60 (6)
(4)	0.00462 (5)	0.28507 (10)	0.24564 (5)	196 (10)	145 (11)	157 (10)	-7 (3)	- 66 (6)	2 (3)
(2)	0.25301 (5)	0-00130 (4)	0.28533 (10)	161 (10)	240 (11)	109 (10)	- 74 (6)	-4(3)	0 (3)
O(6)	0.13299 (32)	- 0-08466 (35)	0.15030 (33)	181 (29)	251 (32)	130 (30)	- 47 (24)	- 29 (25)	-54 (23)
5	0.14435 (33)	0.12989 (34)	-0-08507 (35)	142 (29)	250 (32)	202 (32)	- 20 (26)	- 39 (23)	- 49 (23)
(8)	-0.08038(35)	0.14693 (33)	0.12412 (31)	198 (30)	128 (28)	197 (30)	-1 (22)	- 57 (22)	-33 (24)
<u>(6)</u>	-0.37447 (31)	0-41757 (34)	-0-35569 (31)	180 (29)	236 (31)	73 (27)	- 83 (23)	-41 (24)	- 19 (22)
(10)	-0.35081(32)	-0-37238 (33)	0-41947 (35)	129 (29)	237 (31)	183 (31)	24 (25)	7 (23)	- 99 (23)
(11)	0-41306 (34)	-0.35285 (33)	-0.36571 (33)	148 (30)	130 (28)	249 (31)	-7 (22)	-62 (22)	8 (24)
(Mn <sub>0.983</sub> F(	<sup>20.017</sup> )2O3								ſ
M†	0	0	0	8) 68	$=\beta_{11}$	$=\beta_{11}$	12 (4)	$=\beta_{12}$	$=\beta_{12}$
M	0.28508 (9)	0	-44	109 (10)	229 (9)	157 (9)	0	0	78 (4)
0	0-12913 (19)	0·14708 (18)	-0.08347 (22)	247 (19)	136 (18)	202 (20)	18 (16)	- 131 (13)	- 12 (15)
(Mn <sub>0.37</sub> Fe	9.63)2O3							¢	c
M	0	0	0	127 (10)	$=\beta_{11}$	$=\beta_{11}$	18 (5)	$=\beta_{12}$	$=\beta_{12}$
M	0-28473 (12)	0	-44	172 (13)	179 (11)	160 (11)	0	0	- 36 (6)
0	0.13527 (26)	0-13950 (24)	0·08830 (31)	183 (24)	124 (22)	270 (26)	- 73 (19)	- 19 (19)	50 (21)
* The a † M des	tom numbers are the ignates average catio	same as those of N.n.	orrestam (1967). See a	lso last section c	of Discussion.				

Table 2. Positional and thermal parameters (standard errors)

sities was obtained from each of the two iron-containing specimens.

## **Refinement of the structure**

In the refinement calculations, the Busing, Martin & Levy (1962) least-squares program modified by Ibers, Hamilton, Johnson, Ellison & Levy to include the imaginary part of the anomalous dispersion correction was used. Atomic form factors used were those of Cromer & Waber (1965) for Mn3+ and Fe3+ and those of Tokonami (1965) for O<sup>2-</sup>. Both the real and imaginary parts of the anomalous dispersion corrections (Cromer, 1965) for the cations were used. For  $(Mn_{0.983}Fe_{0.017})_2O_3$ , the changes in atomic form factors from those of Mn<sub>2</sub>O<sub>3</sub> were neglected. For  $(Mn_{0.37}Fe_{0.63})_2O_3$ , the distribution of Mn<sup>3+</sup> and Fe<sup>3+</sup> ions on the two sites was assumed to be random even though it is known (Banks, Kostiner & Wertheim, 1966; Grant et al., 1968) not to be. However, the ionic distribution and the closeness of atomic form factor values for Mn<sup>3+</sup> and Fe<sup>3+</sup> for the same  $\sin \theta / \lambda$  value are such that no attempt was made to refine multipliers.

The structure of  $(Mn_{0.983}Fe_{0.017})_2O_3$  was refined starting with equal weights and isotropic thermal parameters. Structure amplitudes greater than 250 and a few unobserved reflections were given extremely low weights essentially removing these from the refinement. After 3 cycles, anisotropic thermal parameters were introduced and the discrepancy factor came rapidly to 0.02 excluding a few very high and a few unobserved structure amplitudes.

The thermal parameters obtained from the refinement of  $(Mn_{0.983}Fe_{0.017})_2O_3$  were then applied to  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> according to the symmetry of the latter. The positional parameters were started at Norrestam's (1967) results. Eleven large structure amplitudes were given very low weights, as were also 41 low structure amplitudes which appeared, after one iteration, to have been observed larger than they should have been, probably because of radiation streaks not adequately compensated by the Y filter. (These amplitudes are also designated by an asterisk in Table 2.) All other intensities were given  $\sigma = 0.046|F|$  except those with  $|F| \leq$ 20.0 which were all given  $\sigma = 0.9$ . Three least-squares cycles, in which all parameters (a total of 94 including one scale factor) were allowed to vary, brought convergence. The discrepancy factor excluding the 52 lowweight amplitudes is 0.034. Final values of the parameters are given in Table 2. A listing of observed and calculated structure may be obtained from the author upon request.

Starting parameters for  $(Mn_{0.37}Fe_{0.63})_2O_3$  were those from the results of the refinement of  $(Mn_{0.983}Fe_{0.017})_2O_3$ . At first, equal weights were used except that several large amplitudes (indicated by asterisk in Table 3) and unobserved reflections were given low weights. Convergence was very rapid. Final cycles of least-squares calculations were run on both cubic cases with  $\sigma =$ 0.046|F| for all except those with  $|F| \le 20$ , which in both cases were given  $\sigma = 1.0$ . These weighting schemes gave for estimated standard errors of an observation (including all amplitudes) 1.36, 0.90 and 1.17 for  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>, (Mn<sub>0.983</sub>Fe<sub>0.017</sub>)<sub>2</sub>O<sub>3</sub> and (Mn<sub>0.37</sub>Fe<sub>0.63</sub>)<sub>2</sub>O<sub>3</sub> respectively. Discrepancy factors for both (Mn<sub>0.983</sub>Fe<sub>0.017</sub>)<sub>2</sub>O<sub>3</sub> and (Mn<sub>0.37</sub>Fe<sub>0.63</sub>)<sub>2</sub>O<sub>3</sub> are 0.027. Final parameter values and a comparison of calculated with observed amplitudes for these are given in Tables 2 and 3 respectively.

## Table 3. Comparison of calculated and observed amplitudes, $(Mn_{0.983}Fe_{0.017})_2O_3$ and $(Mn_{0.37}Fe_{0.63})_2O_3$ .

t = 0 t + 1 (Cent.) t = 2 t + 3	t = 4 (Cont.)
0.017Fe <sup>3+</sup> 0.63Fe <sup>3+</sup> 0.017Fe <sup>3+</sup> 0.63Fe <sup>3+</sup> 0.017Fe <sup>3+</sup> 0.63Fe <sup>3+</sup> 0.017Fe <sup>3+</sup> 0.63Fe <sup>3+</sup>	0.017Fe <sup>3+</sup> 0.63Fe <sup>3+</sup>
The stration of the stration is the stration of the strategies	A K LEAF LEAF LEAF LEAF
0 2 42 39 35 35 1 6 121 123 125 126 2 2*401 575 490 594 3 4 86 86 88 85	5 9 75 76 73 73
2 2 14 14 13 14 5 4 135 141 128 135 5 5 152 153 154 154 5 59 59 72 72	4 10 98 99 96 100
4 2 43 44 47 50 6 3 133 133 133 134 4 4 34 31 36 27 3 6 53 64 65 61	9 7 42 43 45 46
4 4*385 521 480 555 7 Z Z9 31 55 55 3 5 60 59 68 68 5 6 104 103 96 93	10 6 58 57 56 55
6 67 85 94 91 2 7 118 118 120 121 5 5 16 14 28 22 4 7 60 59 66 66	6 10 31 30 42 39 11 5 31 31 31 30
2 6 52 54 59 60 5 6 65 64 66 64 6 4 35 36 40 41 3 8 80 84 82 83	5 11 43 42 42 42
4 6 46 43 50 50 7 4 68 68 72 69 7 3 32 30 29 30 6 7 122 122 117 121	e = 5
8 2 92 94 90 92 8 3 69 70 72 73 2 8 103 103 104 5 8 93 93 99 102	0.0175+3+ 0.635+3+
2 8 145 149 132 136 3 8 67 67 79 76 6 8 200 216 219 224 9 4 74 81 81 6 6 21 21 20 23 9 2 12 13 18 11 7 5 9 7 4 8 3 4 9 62 61 60 50	h k (F_1   F_1   F_1 ) (F_1
8 4 180 190 178 182 2 9 34 33 31 32 5 7 53 51 37 38 3 10 79 78 68 77	5 6 98 98 102 104
0 10 98 99 98 101 6 7 53 51 47 48 4 8 55 56 66 66 7 8 78 79 72 7	7 6 56 58 65 69
8 6 18 17 40 30 8 5 54 55 63 63 7 3 30 37 36 7 0 37 37 48 43 6 8 112 115 128 112 5 8 47 45 45 46 3 9 40 41 38 35 6 9 42 44 56 56	5 8 102 104 95 99
10 2 107 108 102 105 9 4 33 32 32 33 7 57 57 63 62 10 5 41 43 45 45	7 8 48 49 56 55
10 4 136 142 143 148 1 10 54 53 48 48 6 8 53 53 48 51 11 4 60 60 50 50	9 6 48 49 40 39
+ 10 108 110 97 101 10 3 65 63 63 62 4 70 133 159 165 166 4 11 3 42 45 46 8 8 102 100 113 118 3 10 53 53 59 58 9 5 14 14 33 32 9 8 37 38 33 32	5 10 35 34 28 28
10 6 84 87 74 75 8 7 58 59 67 67 5 9 40 40 52 52 8 9 55 53 56 51	8 9 47 49 44 50
0 12 125 128 125 125 9 6 94 94 98 95 4 10 142 147 138 138 7 10 42 41 43 4	7 10 40 39 42 42
12 2 89 92 106 105 6 9 55 66 69 69 11 3 65 62 70 73 11 6 65 65 60 50	
12 4 90 91 184 109 2 11 11 11 19 17 3 11 (10 8 25 22 6 11 33 32 27 24	1. 1. 1.
10 8 170 174 159 163 5 10 80 70 80 80 10 5 92 93 100 97 41	0.017Fe <sup></sup> 0.63Fe <sup></sup>
4 11 42 43 50 50 6 10 93 94 96 97 0 0175 <sup>34</sup> 0 67	
	7 7 47 46 44 45
0.0177e3 0.637e34 8 9 72 72 68 67 12 113 116 109 115 4 229 256 240 240	8 8 32 32 57 50 85 nr 56 56 8 8
h k Fol Fc Fo Fc 7 10 54 54 51 53 4 12 73 74 71 71 4 5 65 51 57 60	9 7 52 51 53 54 7 9 56 55 54 51
3 2 43 38 26 22 3 12 38 38 32 31 10 8 411 9 21 19 5 6 61 59 53 56	6 10 67 63 67 67
2 J 27 J 25 26 11 6 44 46 53 55 0 10 10 10 11 10 140 5 7 62 61 6 62	1+7
4 3 127 133 133 132 12 5 44 44 43 42 7 11 33 34 29 29 7 67 68 58 59	0.017Fe <sup>3+</sup> 0.63Fe <sup>3+</sup>
5 2 78 77 83 82 13 2 37 35 39 36 6 8 138 142 125 132	N ≥  F <sub>0</sub>    F <sub>0</sub>    F <sub>0</sub>    F <sub>0</sub>
6 9 03 02 /0 67 4 13 CI 11 22 19 9 5 67 65 60 60	7 8 41 41 46 48

### Interionic distances and angles

Interionic distances and angles and their estimated standard errors were calculated with the Busing, Martin & Levy (1964) computer program *ORFFE*. These are shown in Tables 4 and 5. The limits of error in the cation-oxygen distances are 0.006-0.009 Å; in O-O distances, 0.009-0.018 Å, and in oxygen-cation-oxygen and cation-oxygen-cation angles,  $0.3-0.6^{\circ}$ .

## Discussion

## *Relationship between the cubic and orthorhombic structures*

In the case of the cubic structure alone there are two descriptions with the equipoints of Ia3 that give indistinguishable structures. The description usually given for the bixbyite structure has cations in 8(b) and 24(d) and oxygen ions in 48(e), the general positions. For clarity we shall write the representative coordinates of each of the atoms for  $(Mn_{0.983}Fe_{0.017})_2O_3$  in this description:

	Mn(b)	$\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$
(1)	Mn(d) -	$-0.0351, 0, \frac{1}{4}$
	0	0.3791,0.1665,0.3971

Translating by  $\frac{1}{4} \frac{1}{4} \frac{1}{4}$ , we obtain

Mn	0,0,0
Mn	$-0.2851, \overline{\frac{1}{4}}, 0$
0	0.1291, -0.0835, 0.1471

## Table 4. Interionic distances in Å and angles in degrees

(2)

#### (a) $(Mn_{0.37}Fe_{0.63})_2O_3$ , (b) $(Mn_{0.983}Fe_{0.017})_2O_3$ , (c) analogous average from $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>.

	Polyhedron about cation in $8(a)$			Subtended angle				
	<i>(a)</i>	<i>(b)</i>	( <i>c</i> )	<i>(a)</i>	<i>(b)</i>	(c)		
(Mn, Fe) - O(6)	2.009(2)	2.003(2)	2.002(3)		.,			
O-O(6)	2.668 (4)	2·703 (3)	2.704 (4)	83·2 (1)	84.9 (1)	84.9 (1)		
O-O(6)	3.005 (4)	2·957 (4)	2.957 (5)	96·8 (1)	95·1 (1)	95·1 (1)		
	Polyhedro	n about catio	n in 24( <i>d</i> )					
(Mn, Fe)-O(2)	2.147 (3)	2.242 (2)	2.243 (3)					
(Mn, Fe) - O(2)	1.930 (3)	1.898 (2)	1.898 (3)					
(Mn, Fe) - O(2)	2.033 (3)	1.987 (2)	1.988 (3)					
$\dot{O}-\dot{O}(2)$	2.600 (4)	2·578 (3)	2·580 (5)	76.9 (1)	74.9 (1)	74.9 (1)		
O-O(2)	2.600 (4)	2·578 (3)	2.580 (5)	82·0 (1)	83·1 (1)	83·2 (1)		
O-O(2)	2.668 (4)	2.703 (3)	2.703 (3)	79·3 (1)	79·2 (1)	79·3 (1)		
O - O(2)	3.391 (4)	3.481 (3)	3.483 (4)	112.4 (1)	114·2 (1)	114.3 (1)		
O-O(2)	3.048 (3)	3.055 (2)	3.055 (5)	96·6 (1)	94·8 (1)	94.7 (1)		
0-0	2.726 (6)	2.765 (4)	2.766 (5)	89.8 (2)	93·6 (1)	93.6 (2)		
0-0	3.288 (5)	3.109 (4)	3.109 (5)	108.0 (2)	103.0 (1)	102.9 (2)		
	Cation-	-oxygen-catio	n angles					
d-O-a(2)	96.7 (1)	93·8 (1)	93.8 (1)					
(2)	129.7 (2)	132·4 (1)	132.3 (2)					
(2)	100.4 (1)	$102 \cdot 1$ (1)	102·1 (1)					
d - O - d(4)	122.8 (1)	119·8 (1)	119·7 (2)					
(4)	104·0 (1)	106·9 (1)	106·9 (1)					
(4)	96·7 (1)	94·9 (1)	94·9 (1)					

Notes: (1) Standard errors in parentheses apply to the last digits.

(2) There are six of each a-O-d angle involved in the polyhedron about the ions in the (a) sites.

However, this arrangement is not compatible with the Ia3 space group equipoints; to make it so, y and z must be interchanged, thus

(3) 
$$\begin{array}{c} Mn(a) & 0,0,0\\ Mn(d) & -0.2851,0,\frac{1}{4}\\ & 0.1291,0.1471,-0.0835 \end{array}$$

The two sets of parameters, (1) and (3), give exactly the same values of structure amplitude, but there must be an interchange of axes and therefore indices, *e.g.*  $F_{hkl}(1) = F_{khl}(3)$ .

There are two ways in which sets (1) and (3) may go into the orthorhombic structure. One is by way of set (2), that is, the translation  $(\frac{1}{4}, \frac{1}{4}, \frac{1}{4})$  from set (1). This is the description given by the parameters for  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> in Table 2 in space group *Pcab*. Set (3) is equivalent to this because an interchange of y and z coordinates and of b and c simply alters the space group designation to the equivalent *Pbca*, used by Norrestam (1967) (see also last section of *Discussion*).

There is another, quite different way in which the structure *might* transform from cubic to orthorhombic. The set (1) might go directly into the orthorhombic structure without translation, *i.e.* the Mn<sup>3+</sup> ions in 8(*b*) might go into a set of general positions in the orthorhombic space group. This case *is* distinguishable from the above. Thus while our 'guess' (Grant *et al.*, 1968) regarding distinguishing these two structures was not correct, the possibility that the 25 °K transformation of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> might involve a shift in symmetry center, *i.e.* to the structure with all atoms in general positions (Grant *et al.*, 1968), is a valid suggestion. It should be recalled that the *powder* data at 6.5 °K showed no noticeable change in structure, even though

the transformation at 25°K appears to be first order (Grant *et al.*, 1968; Geller & Espinosa, 1970).

#### Phase transition from orthorhombic to cubic

There are two independent pieces of experimental evidence which indicate that the orthorhombic-to-cubic transition which occurs at 302°K is higher than first order. X-ray powder diffraction photographs of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> were taken in the temperature range 81 to 702°K. No discontinuity in lattice constant or volume was observed. The plot of lattice constant vs. temperature in the important range is given in a previous paper (Geller & Espinosa, 1970). Mössbauer effect spectroscopic measurements were made on specimens  $(Mn_{0.972}Fe_{0.028})_2O_3$  and  $(Mn_{0.94}Fe_{0.06})_2O_3$  which have orthorhombic-to-cubic transitions at 260 and 165°K respectively. For each, the quadrupole splittings of Fe<sup>3+</sup> ions in the  $8(b)^*$  and 24(d) sites increased markedly but continuously with decreasing temperature below the transition temperatures (see Fig. 5 of Grant *et al.*.. 1968). No discontinuities occurred in either the isomer, shifts or absorption line widths (see Figs, 6 and 7, respectively, of Grant et al., 1968). In view of the observed nature of this orthorhombic  $\rightarrow$  cubic transformation of the Mn<sub>2</sub>O<sub>3</sub> it was pleasantly surprising that in no case did we find the crystals to be twinned.

#### Comparison of the three structures

Among sesquioxides of the trivalent ions of Ti, V, Cr, Mn, Fe and Ga,  $Mn_2O_3$  is the only one that does not have a corundum-type structure. This is not a result of ionic size because  $Mn^{3+}$  is slightly smaller than

\* 8(a) in the description of Table 2.

Polyhedron about atom 1		Polyhedron about atom 3		Polyhedron about atom 4			Polyhedron about atom 5				
Atoms	L	O-Mn-O	Atoms	Z	∠O-Mn-O	Atoms	4	∠O-Mn-O	Atoms	Z	O-Mn-O
1-6 (2)	2.050		39	2.297		4—7	2.268		58	2.267	
1-7 (2)	1.996		3—6	2.190		4–10	2.223		5-11	2.215	
1 - 8(2)	1.963		38	2.001		4—9	1.992		5-10	2.006	
6-8 (2)	2.693	84.3	3-11	1.976		46	1.981		5—7	1.972	
7-8 (2)	2.702	86.1	37	1.907		48	1.908		5—9	1.911	
6-7 (2)	2.716	84.3	3-10	1.889		4–11	1.888		5—6	1.883	
7-8 (2)	2.894	93.9	6–11	2.569	75.9	6–10	2.568	75.1	7-11	2.577	75.7
6-8 (2)	2.977	95.7	89	2.593	73.8	7—9	2.590	74.6	8-10	2.585	74.2
6-7 (2)	3.000	95.7	7–11	<b>2·</b> 577	83.1	6-11	2.569	83·1	6–10	2.568	82.6
			8–10	2.585	83.3	89	2.593	83.3	7—9	2.590	83.7
Polyhedron	about a	tom 2	6—8	2.693	79·8	9–10	2.689	79·1	10-11	2.703	79.5
2 - 11(2)	<b>2·0</b> 47		9–11	2.715	78.5	6—7	2.716	<b>79</b> ·1	7—8	2.702	78.9
2-10(2)	1.998		6—7	3.465	115.3	10-11	3.470	114.9	9-11	3.469	114.3
2-9 (2)	1.960		9-10	3.511	113.6	7—8	3.502	113.7	6—8	3.483	113.8
9-10 (2)	2.689	85.6	6–10	3.014	95.0	8-10	3.058	95·2	6–11	3.011	94.2
10-11 (2)	2.703	83.8	7—9	3.090	94·1	7-11	3.061	94.4	8—9	3.098	95.3
9-11 (2)	2.715	85.3	7–10	<b>2</b> ·766	93.5	8-11	2.765	93·5	6—9	2.766	93.6
9-10 (2)	2.905	94.4	8-11	3.111	102.9	69	3.108	102.9	7–10	3.110	102.8
9-11 (2)	2.948	94.7									
10-11 (2)	3.010	96.2									

Table 5. Interionic distances in Å and angles in degrees,  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>

Notes: (1) For atom identification, see Tables 2 and 4.

(2) Estimated standard errors are: 0.002 Å for a Mn-O distance, 0.004-0.005 Å for an O-O distance and 0.1-0.2° for an angle.

Fe<sup>3+</sup> (Geller, 1957), smaller than both Ti<sup>3+</sup> and V<sup>3+</sup> and larger than Cr<sup>3+</sup> and Ga<sup>3+</sup> (Geller, 1957; see also Shannon & Prewitt, 1969). It is very likely a result of the large Jahn–Teller distortion (Dunitz & Orgel, 1957) associated with Mn<sup>3+</sup> (Geller *et al.*, 1967). It is unlikely that any other oxide (*i.e.* not a solid solution with Mn<sub>2</sub>O<sub>3</sub>) will ever be found to have the orthorhombic structure of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub>. The cubic strucure allows less distortion than the orthorhombic (see Tables 2, 4 and 5).

At a substitution of about 0.75 cation % Fe<sup>3+</sup> for Mn<sup>3+</sup>, the structure becomes cubic at room temperature (Grant *et al.*, 1968). However, the structure of  $(Mn_{0.983}Fe_{0.017})_2O_3$  was refined because of the immediate availability of a spherical single crystal from previous experiments. The additional one cation % Fe<sup>3+</sup> does not make a measurable structural difference as indicated by the results shown in Table 4: in every case of distance and angle, the average from the  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> differs by one standard deviation or much less from the analogous distance or angle in

## $(Mn_{0.983}Fe_{0.017})_2O_3$ .

In the cubic structure the Mn(a)-O distances (Table 4) are all equal, 2.003 Å. while the analogous (six nonequivalent) Mn-O distances (Table 5) in the orthorhombic structure range from 1.960–2.050 Å. In the cubic structure the Mn(d)-O distances are of three lengths ranging from 1.987-2.242 Å, while in the orthorhombic structure the analogous (18 nonequivalent) distances range from 1.883–2.297 Å. It should be kept in mind that if we accept the results on  $(Mn_{0.983}Fe_{0.017})_2O_3$ to represent those just above the transition of  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> at 302 °K, these differences in the range of distances occur for a difference of only 7°K. One is then led to wonder why, if the Mn<sup>3+</sup> prefers the greater number of degrees of freedom, it transforms to the cubic structure at such a low temperature. There is the possibility that in the cubic structure and especially in the high symmetry a (or b) sites, there is electronic disorder of some sort. The disorder could be dynamic(Gyorgy,LeCraw&Sturge,1966;Iida,Mizushima, Yamada & Iizuka, 1968) or static – that is, all the Mn(a)-O distances may not actually be equal but so distributed as to give a statistically cubic crystal. Some disorder may also exist about the cations in the orthorhombic structure decreasing with decreasing temperature.

The distortion in the orthorhombic structure increases considerably with decreasing temperature as is established from the measurements of quadrupole splittings (Grant *et al.*, 1968). These splittings increase continuously down to liquid N<sub>2</sub> temperature, but there is little, if any, tendency for the lines in the powder spectra to resolve into sets of three and two. Thus the increase in distortion with decreasing temperature is considerably larger than the differences in distortion caused by non-equivalent ions originating from the same set of equipoints of the cubic structure. Also the lattice constants of Mn<sub>2</sub>O<sub>3</sub> itself reach near constancy at about  $150^{\circ}$  K; thus the lattice constants do not in this case give an indication of changes occurring in the structure, but there is no question that the quadrupole splittings do (see for example, Grant, 1969; Colville, 1970).

Of sesquioxides with the C-type structure, refinements, with accuracy comparable with the present ones, were done on Sc<sub>2</sub>O<sub>3</sub> (Geller, Romo & Remeika, 1967, 1968; Norrestam, 1968), In<sub>2</sub>O<sub>3</sub> (Marezio, 1966) and Y<sub>2</sub>O<sub>3</sub> (Paton & Maslen, 1965; O'Connor & Valentine, 1969\*). For  $Sc_2O_3$  and  $In_2O_3$ , the average *d*-site cation-oxygen distance is equal  $(\pm 0.01 \text{ Å})$  to the *b*-site cation-oxygen distance; for Y<sub>2</sub>O<sub>3</sub>, Paton & Maslen (1965) give for the average Y(d)-O distance a value 0.04 Å greater than Y(b)-O, while O'Connor & Valentine (1969) find that they are equal. In  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> the average of the Mn(c)-O distances is 0.041 Å greater than the average of the Mn(a)-O and Mn(b)-O distances. In  $(Mn_{0.983} Fe_{0.017})_2O_3$ , the difference between analogous distances is 0.039 Å, while the analogous difference in  $(Mn_{0.37}Fe_{0.63})_2O_3$  decreases to 0.028 Å. There is no significant difference among the overall average cationoxygen distances.

It is quite clear that saturation of the  $Mn_2O_3$  structure with Fe<sup>3+</sup> changes one of the cation-oxygen distances drastically (see Table 4). The range width of Mn-O distances is reduced from 0.344 Å in  $(Mn_{0.983}Fe_{0.017})_2O_3$  to 0.217 Å in  $(Mn_{0.37}Fe_{0.67})_2O_3$ . For Sc<sub>2</sub>O<sub>3</sub> the analogous value is 0.08 Å;for In<sub>2</sub>O<sub>3</sub>, 0.10 Å; for Y<sub>2</sub>O<sub>3</sub>, 0.09 or 0.10 Å. The largest range is found in  $\alpha$ -Mn<sub>2</sub>O<sub>3</sub> itself (see Table 5), namely 0.414 Å. Thus it is evident that the Mn<sup>3+</sup> ion behaves quite differently from the other cations in the *C*-type structure. Especially, these results emphasize that Mn<sup>3+</sup> requires more distorted surroundings.

#### Magnetic aspects

 $Mn_2O_3$  has an antiferromagnetic transition at 80 °K (King, 1954; Meisenheimer & Cook, 1959; Geller et al., 1967; Grant et al., 1968) and another antiferromagnetic transition at 25°K (Geller et al., 1967; Grant et al., 1968; Chevalier, Roult & Bertaut, 1967†); the latter appears to be first order. Replacement of Mn<sup>3+</sup> by Fe<sup>3+</sup> causes a reduction in all transition temperatures. The lower antiferromagnetic one decreases rapidly with Fe<sup>3+</sup> substitution; at 0.75 cation % Fe<sup>3+</sup>. it occurs at 19°K and it is not observed in a specimen with 2.8 cation % Fe<sup>3+</sup> substitution (Grant et al., 1968). Smaller ions, however tend to raise the temperature of the lower transition (Geller & Espinosa, 1970). Because of this trend, the reordering would appear to involve some atomic displacements in accord with the aforementioned suggestion regarding this transition.

<sup>\*</sup> Comments made by these authors relative to interatomic distances in bixbyite are not supported by the results of the present work.

<sup>&</sup>lt;sup>†</sup> The lower temperature transition was found by neutron diffraction, but the transition temperature reported is not in accord with that determined in our experiments.

As the temperature decreases below the cubic to orthorhombic transition temperature the quadrupole splittings associated with the ions in the two kinds of sites increase continuously (Grant, 1969). Thus it is probable that the room temperature structures (especially of the cubic ones which transform to the orthorhombic) can be only symptomatic of what occurs at the lower temperatures. The suggestion is that the onset of magnetic ordering is somehow associated with the amount of distortion.

There appears to be a close association of the magnetic ordering of the orthorhombic phases,  $(Mn_{1-x}Fe_x)_2O_3 \ 0 \le x \le 0.09$ , with the Jahn-Teller distortion of the Mn<sup>3+</sup> ions. The substitution of Fe<sup>3+</sup> for Mn<sup>3+</sup> tends to reduce the distortion (see Table 4) and the magnetic ordering temperature in the orthorhombic region (Grant et al., 1968). In the orthorhombic region, substitution of the diamagnetic ion Ga<sup>3+</sup> for Mn<sup>3+</sup> has about the same effect on the upper Néel temperature as the same amount of Fe<sup>3+</sup>; there is a strong indication that above 38 cation % Ga<sup>3+</sup>, well into the cubic region, there will be no further magnetic ordering (Geller & Espinosa, 1970). This is in contrast to  $(Sc_{0.5}Fe_{0.5})_2O_3$ , with the same structure, which has a magnetic ordering temperature of approximately 35°K (Geller, Williams & Sherwood, 1961\*). There is only a small increase in Néel temperature in the cubic region of the  $(Mn_{1-x}Fe_x)_2O_3$  system, *i.e.* from 9 to 63 cation % Fe<sup>3+</sup> (Grant et al., 1968).

There are no a-O-a type magnetic interactions (see Table 4) and it would therefore seem that the magnetic ordering in the a-type sites is tied intimately to that in the d-type sites. Also there are twice as many d-O-d as d-O-a interactions (Table 4). Thus it would appear that magnetic ordering could be attained with paramagnetic ions exclusively in d-type sites, but not with paramagnetic ions exclusively in a-type sites.

It has been shown (Geller & Espinosa, 1970) that the substitution of  $Cr^{3+}$  for  $Mn^{3+}$  ion in  $Mn_2O_3$  does not have as large an effect as  $Fe^{3+}$  ion substitution on the Néel temperature. For 8 cation %  $Cr^{3+}$  substitution the upper Néel temperature,  $T_{NI}$ , is 71°K, while it is down to 42°K for 8 cation %  $Fe^{3+}$ ; at 12 cation %  $Cr^{3+}$ , the upper Néel temperature,  $T_{NI}$ , is reduced only to 68°K. The explanation hypothesized for this is the greater compatibility of  $Cr^{3+}$ , which has empty  $e_g$ orbitals, with  $Mn^{3+}$  which has one electron in the  $e_g$ orbitals as opposed to any ion with a filled, half-filled or completely empty *d*-shell. It appears that as a result of gaining further insight into the structures, this explanation may now be extended.

Probably because of the Cr<sup>3+</sup> electronic configura-

tion,\* the range of Cr<sup>3+</sup> substitution in which the structure may still be orthorhombic (at temperatures >  $0^{\circ}$ K) is wider than for all the other substituent ions (see Geller & Espinosa, 1970). Thus as long as the structure can remain orthorhombic, the Mn<sup>3+</sup> ions in the more symmetric sites can have their distorted surroundings with which the magnetic ordering must be importantly linked. There is some evidence to support such a hypothesis. An extrapolation of the line through the Néel temperatures of cubic phases, *i.e.* for x > 0.09, to x=0 gives a Néel temperature of ~26°K (see Fig. 3 of Grant et al., 1968). This implies that if pure Mn<sub>2</sub>O<sub>3</sub> had the cubic structure it would have only about one-third the Néel temperature it actually has. There is also the possibility that the spins of Mn<sup>3+</sup> ions in the high symmetry (a) sites are not ordered in the cubic antiferromagnetic phases.

# Comparison of present and Norrestam's results for $\alpha\text{-}Mn_2O_3$

The transformation 100|001|010 takes the  $Mn_2O_3$ positional parameters given in Table 2 into those of Norrestam. This implies that the transformation 100|001|010 takes our axes and reflexion indices into those of Norrestam. There is agreement for the transformation of indices (obtained by comparing observed structure amplitudes) and for the transformation of our *b* to Norrestam's *c* axis, both of which equal 9.4233 Å. However, our *a* axis of 9.4157 Å transforms to his of 9.4118 Å, and our *c* axis of 9.4047 Å transforms to his of 9.4177 Å. Not only do the lengths not agree but the size order is reversed.

The reasons for these discrepancies are not known. They are not a result of the different working temperature: Norrestam's was  $27.5^{\circ}$ , ours  $25^{\circ}$ C. According to our measurements of lattice constant *versus* temperature (Geller & Espinosa, 1970), neither of the two smaller axes ever reaches 9.4177 Å below the transition temperature. Further, the average value of our axes at  $25^{\circ}$ C is  $9.4146 \pm 0.0003$  Å, exactly equal to the lattice constant of  $(Mn_{0.983}Fe_{0.017})_2O_3$  (see Table 1). Norrestam's average value is  $9.4176 \pm 0.0007$  which seems much too high.

Norrestam's data covered a larger range of  $\sin^2\theta$ , namely to 0.6 while our data went only to  $\sin^2\theta = 0.25$ ; we observed many more of the faint reflections in the range covered. Although the *R* value is slightly higher than Norrestam's, the estimated standard errors in positional parameters and Mn–O distances are half his. There are some large differences in thermal parameters especially for  $\beta_{ij}$ ,  $i \neq j$ .<sup>†</sup> Norrestam's  $\sigma$  values for these are in some cases 4 times as large as those given in

<sup>\*</sup> In the earlier paper, Geller *et al.* (1961) reported magnetic transitions at  $7 \pm 1$  °K and 'possibly one at about 35 °K'. Recent Mössbauer effect measurements by Grant in this laboratory on a new (Sc<sub>0-5</sub>Fe<sub>0-5</sub>)<sub>2</sub>O<sub>3</sub> specimen confirm the higher temperature transition. However, susceptibility and Mössbauer measurements do not confirm the lower one.

 $<sup>\</sup>ast$  This can include the effect of electronic configuration on site preference.

<sup>†</sup> The Busing-Levy program refines the parameters of

 $T = \exp\left(-h^2\beta_{11} - k^2\beta_{22} - l^2\beta_{33} - 2hk\beta_{12} - 2hl\beta_{13} - 2kl\beta_{23}\right).$ 

Norrestam's  $\beta_{ij}$  values contain the factor of 2. However, the differences referred to take this into account.

Table 2. Further, there is perhaps a little more reasonableness to the  $\beta$  values given in Table 2 of the present paper. There are some differences in positional parameters and interatomic distances, but in view of Norrestam's larger estimated standard errors, these do not appear to be statistically significant.

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